

# Entropy-Based Dynamic Complexity Metrics for Service-Oriented Systems

Chengying Mao, Changfu Xu

School of Software and Comm. Eng., Jiangxi University of Finance and Economics, Nanchang, China

E-Mail: maochy@yeah.net





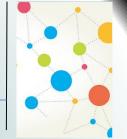
#### **Outline**



- Background
- Entropy-based dynamic complexity metrics framework
- Two models and entropy definition
- Experimental analysis
- Conclusions



#### Background



- The complexity analysis of service system is mainly from the static aspect, and the dynamic complexity measurement has not attracted enough attention yet.
- Two core issues dynamic complexity metric for service system:
  - which factors to consider of the dynamic complexity of service system.
  - How to model dynamic complexity metrics of service system.



#### Background (cont.)

- Some metrics about the complexity of a service system have been deeply investigated from two aspects of control structure and information flow:
  - Control flow.
  - Data flow.
  - Interface.
- In difference, we consider that the dynamic complexity of a service system with execution traces.



### Entropy-Based Dynamic Complexity Metrics Framework



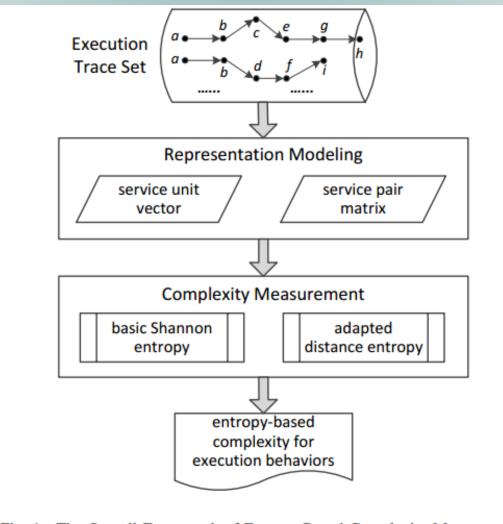


Fig. 1. The Overall Framework of Entropy-Based Complexity Measurement for the Dynamic Execution Behaviors of a Service System



#### **Two Models and Entropy Definition**



Two Models for Execution Traces

Given a service system has six services, in which the services are from  $s_1$  to  $s_6$ ,  $T_1 = \langle s_1, s_2, s_4, s_2, s_4, s_6 \rangle$  and  $T_2 = \langle s_1, s_5, s_6 \rangle$  are two possible traces. Then the two traces can be represented to the corresponding **service unit vector** and **service pair matrix** models as below:

Catas	Service unit vector							
Categ.	<b>S</b> 1	<b>S</b> <sub>2</sub>	<b>S</b> 3	<b>S</b> 4	<b>S</b> 5	<b>S</b> 6		
<i>T</i> <sub>1</sub>	1	1	0	1	0	1		
<i>T</i> <sub>2</sub>	1	0	0	0	1	1		

	Service pair matrix								
	S <sub>1</sub> S <sub>2</sub> S <sub>3</sub> S <sub>4</sub> S <sub>5</sub> S <sub>6</sub>								
<b>S</b> 1	0	1	0	0	1	0			
<b>S</b> <sub>2</sub>	0	0	0	1	0	0			
<b>S</b> 3	0	0	0	0	0	0			
S <sub>4</sub>	0	1	0	0	0	1			
<b>S</b> 5	0	0	0	0	0	1			
<b>S</b> 6	0	0	0	0	0	0			



#### Two Models and Entropy Definition (cont.)



- Two definition of entropy:
  - 1) Shannon Entropy

$$H_s = -\sum_{i=1}^m p_i \cdot \log p_i. \tag{1}$$

in which, m is the number of trace category in real application scenarios, for each trace category, its occurrence probability can be counted as  $p_i$  ( $1 \le i \le m$ ).



#### Two Models and Entropy Definition (cont.)



#### 2) Adapted Distance Entropy

$$H_d = \frac{W}{|T|} \times \left(-\sum_{i=1}^{|T|} \frac{w_i}{W} \cdot \log \frac{w_i}{W}\right), \tag{2}$$

in which,  $w_i$  is the average of the distance from  $T_i$  to other (|T| - 1) traces.  $W = \sum_{i=1}^{|T|} w_i$ . T is the execution trace set of a service system.



#### A running example

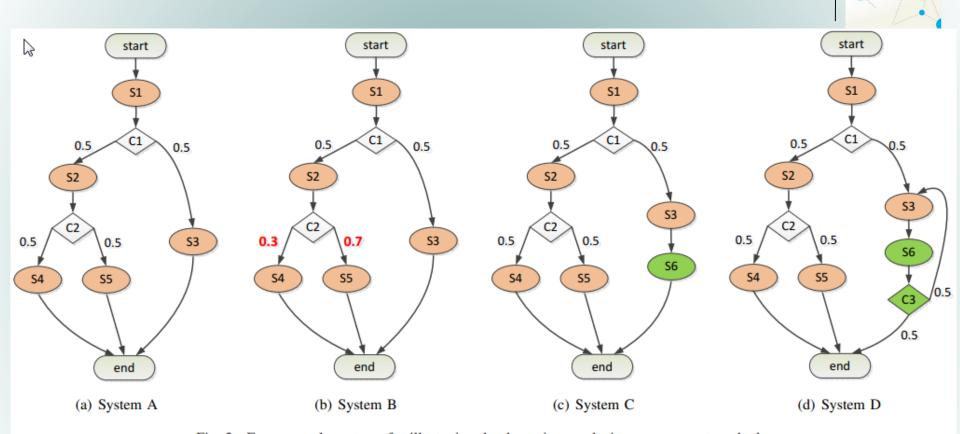


Fig. 2. Four example systems for illustrating the dynamic complexity measurement methods

◆ System Complexity Relation: D > C > A > B.





TABLE I THE EXECUTION TRACES OF FOUR SERVICE SYSTEM ( |T|=20 )

System	Category of Traces	Execution Traces	Occurrence Number
	$C_{A1}$	$s_1 \rightarrow s_2 \rightarrow s_4$	5
A	$C_{A2}$	$s_1 \rightarrow s_2 \rightarrow s_5$	5
	$C_{A3}$	$s_1  o s_3$	10
	$C_{B1}$	$s_1 \rightarrow s_2 \rightarrow s_4$	3
B	$C_{B2}$	$s_1 \rightarrow s_2 \rightarrow s_5$	7
	$C_{B3}$	$s_1 \rightarrow s_3$	10
	$C_{C1}$	$s_1 \rightarrow s_2 \rightarrow s_4$	5
C	$C_{C2}$	$s_1 \rightarrow s_2 \rightarrow s_5$	5
	$C_{C3}$	$s_1 \rightarrow s_3 \rightarrow s_6$	10
	$C_{D1}$	$s_1 \rightarrow s_2 \rightarrow s_4$	5
D	$C_{D2}$	$s_1 \rightarrow s_2 \rightarrow s_5$	5
	$C_{D3}$	$s_1 \rightarrow s_3 \rightarrow s_6$	5
	$C_{D4}$	$s_1 \rightarrow s_3 \rightarrow s_6 \rightarrow s_3 \rightarrow s_6$	5



#### TABLE II THE SERVICE UNIT VECTORS OF FOUR SERVICE SYSTEMS

Sys.	Categ.	Service Unit Vector						Num.	Prob.
Sys.	Categ.	$s_1$	$s_2$	$s_3$	$s_4$	$s_5$	$s_6$	rvuiii.	1100.
	$C_{A1}$	1	1	0	1	0	0	5	0.25
A	$C_{A2}$	1	1	0	0	1	0	5	0.25
	$C_{A3}$	1	0	1	0	0	0	10	0.5
	$C_{B1}$	1	1	0	1	0	0	3	0.15
В	$C_{B2}$	1	1	0	0	1	0	7	0.35
	$C_{B3}$	1	0	1	0	0	0	10	0.5
	$C_{C1}$	1	1	0	1	0	0	5	0.25
C	$C_{C2}$	1	1	0	0	1	0	5	0.25
	$C_{C3}$	1	0	1	0	0	1	10	0.5
D	$C_{D1}$	1	1	0	1	0	0	5	0.25
	$C_{D2}$	1	1	0	0	1	0	5	0.25
	$C_{D3}$	1	0	1	0	0	1	10	0.5





TABLE III
THE SERVICE PAIRS OF FOUR SERVICE SYSTEMS

					e Pair				
System	Category			Number	Probability				
of	of Traces	$(s_1, s_2)$	$(s_1,s_3)$	$(s_2,s_4)$	$(s_2,s_5)$	$(s_3,s_6)$	$(s_6,s_3)$	Number	Trobability
	$C_{A1}$	1	0	1	0	0	0	5	0.25
A	$C_{A2}$	1	0	0	1	0	0	5	0.25
	$C_{A3}$	0	1	0	0	0	0	10	0.5
	$C_{B1}$	1	0	1	0	0	0	3	0.15
В	$C_{B2}$	1	0	0	1	0	0	7	0.35
	$C_{B3}$	0	1	0	0	0	0	10	0.5
	$C_{C1}$	1	0	1	0	0	0	5	0.25
C	$C_{C2}$	1	0	0	1	0	0	5	0.25
	$C_{C3}$	0	1	0	0	1	0	10	0.5
	$C_{D1}$	1	0	1	0	0	0	5	0.25
D	$C_{D2}$	1	0	0	1	0	0	5	0.25
	$C_{D3}$	0	1	0	0	1	0	5	0.25
	$C_{D4}$	0	1	0	0	1	1	5	0.25



**TABLE V** 

The measure result based on four dynamic complexity metrics

Model	Motric	Service-oriented system					
Model	Metric	Α	В	С	D		
Service unit	$H_s(*, suv)$	1.5	1.44	1.5	1.5		
vector	$H_d(*, suv)$	1.4212	1.3828	1.6055	1.6055		
Service pair	$H_s(*,spm)$	1.5	1.44	1.5	2		
matrix	$H_d(*,spm)$	1.4212	1.3828	1.6055	1.8628		

• Only  $H_d(*,spm)$  metric result is consistent with the real dynamic complexity relation of four systems: D > C > A > B.



#### **Experimental Analysis**



#### Experiment Setup

An online travel service system is used for the simulation analysis. As shown in Figure 3. For each version of the service system, |T| = 100 execution traces are simulated and the experiment in each case is

repeated 1000 times.

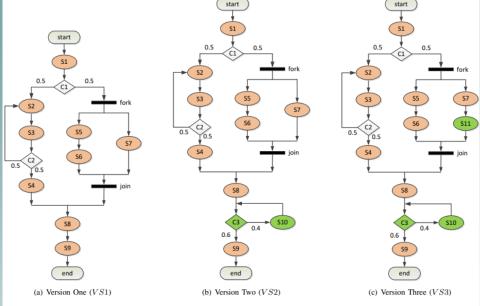


Fig. 3. The business logic of an online travel service system



#### **Experimental Results**



Suggestions on selection measurement method

TABLE VI

THE MEASUREMENT RESULTS OF THE ONLINE TRAVEL SERVICE SYSTEM

Model	Metric	System Version				
Iviouci	Wictife	VS1	VS2	VS3		
service unit	$H_s(*, suv)$	0.9965	1.9518	1.9519		
vector	$H_d(*, suv)$	2.4456	3.0216	3.2128		
service pair	$H_s(*,spm)$	2.0817	3.4863	3.6342		
matrix	$H_d(*,spm)$	3.7762	4.8434	5.0267		

 $H_d(*,spm)$  is the best measurement method.



#### **Conclusions**



- Main contributions:
  - 1) Two representation models;
  - 2) Adapted distance entropy;
  - 3) Four dynamic complexity metrics.
- According to the experimental analysis, the results show that the above two models and two entropies are all suitable to depict the dynamic complexity of a service system. Among them, the combination of service pair matrix and the adapted distance entropy is the best measurement method.





## Thanks for Your Attendance! Any Question?

Contact: maochy@yeah.net

